

# UWB Communication using Compressed Sensing

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## Theoretical Background

### Motivation

Ultra-wideband (UWB) wireless technology advantages:

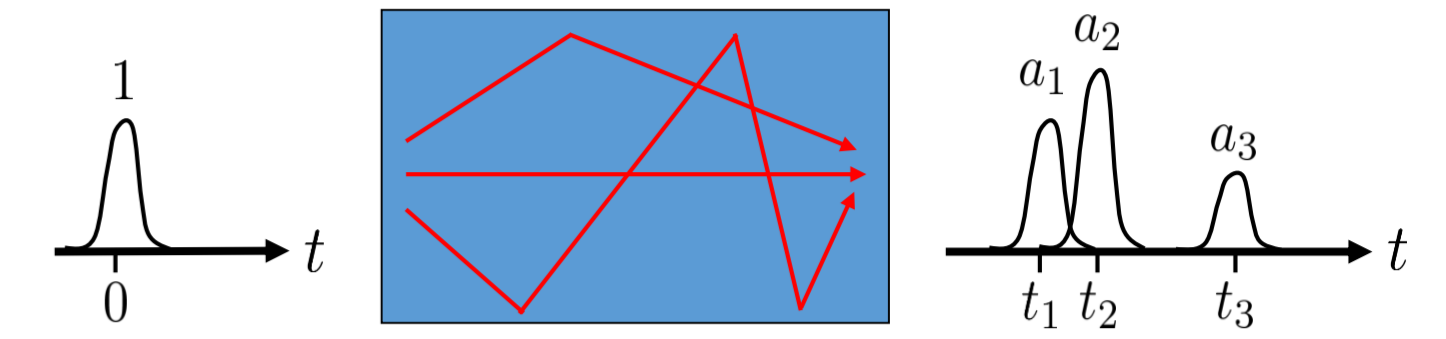
- High data rate
- Frequency diversity can be exploited
- FCC Unlicensed commercial deployment due to low transmitted spectral power density [dBm/Hz]

Restrictions: Short range and High rate ADC is needed

**We propose sub-Nyquist hardware implementation for channel estimation and data detection, by exploiting the sparse nature of the channel response**

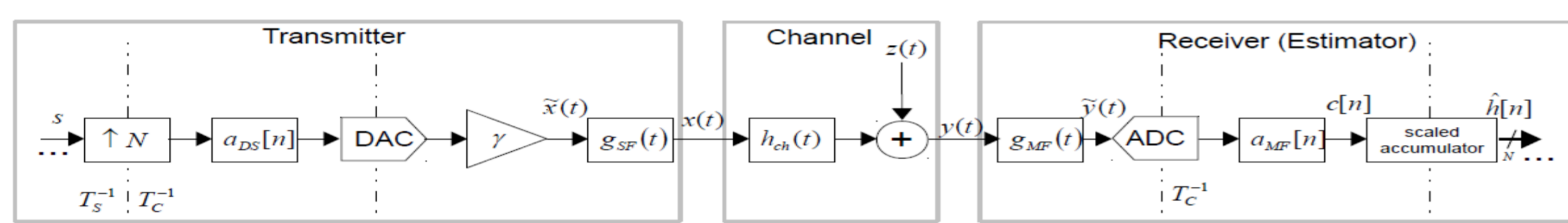
### Channel Model

- Packet based wireless communication, during which the channel is linear time invariant
- The channel contains L resolvable echoes of the input with gain  $a_l$ . Channel response:  $h_{ch}(t) = \sum_{l=1}^L a_l \delta(t - \tau_l) + z(t)$
- Zero mean additive white circular symmetric Gaussian noise is added  $z(t)$
- The parameters  $\{a_l, \tau_l\}$  are unknown to the transmitter and the receiver
- We consider IEEE 802.15.4a channel model, particularly sparse CM1 – Line of Sight Residential
- Our goal is estimating  $H_{ch}(f)$  in order to make data detection possible



### Nyquist Channel Estimation

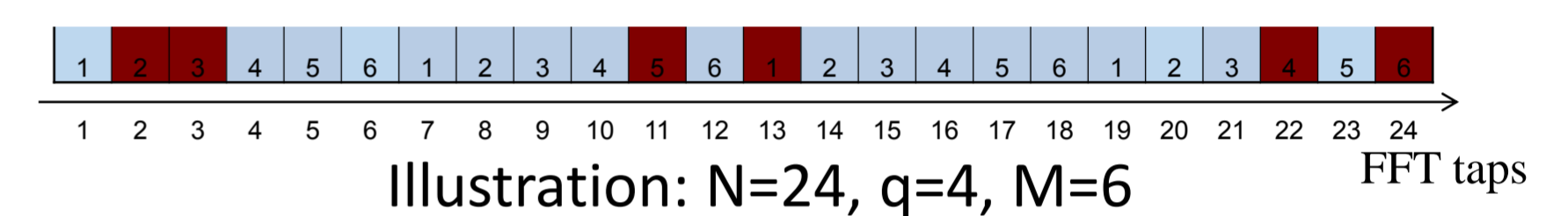
- Transmitter uses a trinary  $\{-1, 0, 1\}$  direct sequence (DS)  $a_{DS}[n]$  which is  $N=511$  chips length to spread spectrum data symbols  $\sim 1$ Mbps known training sequence (for channel estimation) or data (for data detection) is multiplied by the direct sequence and sent in 500MHz DAC
- Transmitted signal is:  $x(t) = \gamma \sum_{i \in \mathcal{L}} s_i \sum_{m=0}^{N-1} g_{SF}(t - mT_c - iNT_c) a_{DS}[m]$



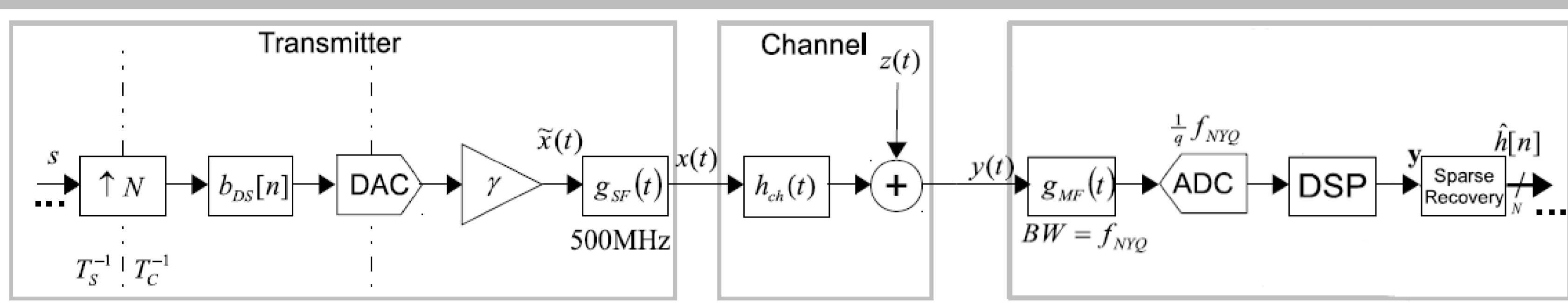
- Complying Nyquist sampling rate requires a high rate ADC
- For channel estimation, an accumulator is used to estimate the channel
- For data detection, rake receiver uses estimated channel

### Sub-Nyquist Channel Estimation

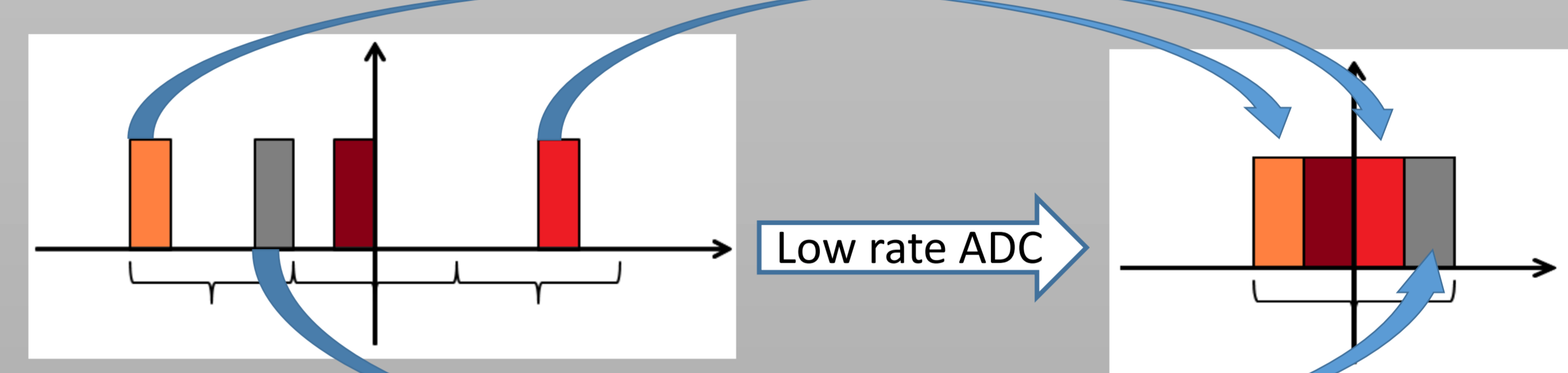
- We want to sample less bands (q time slower than Nyquist), yet maintain the frequency selectivity to some degree
- Transmitter uses signal whose frequency support is a subset  $\mathcal{L}$  of the full bandwidth
- The transmitter will transmit only on M FFT coefficients that are selected by masking DS  $b_{DS} = IFFT_N\{FFT_N\{a_{DS}\}[k], k \in \mathcal{L}\}$
- Sampling is performed by a low rate ADC
- Use sparse recovery (e.g. OMP) to reconstruct the sparse signal
- Seeking wide frequency aperture alongside a single analog branch Foldable method was chosen where we aliases through sampling
- The N taps are split into q groups of size M
- Active set is chosen to be self foldable, such that after sampling by  $1/q$  Nyquist rate, all active coefficients are retraceable:  $\mathcal{L} \cap \{m + M \cdot i\}_{i=0}^{q-1}$  for  $m = 0, \dots, M - 1$



### Sub-Nyquist Model



### Foldable Sampling - One sampler $\frac{1}{q} f_{NYQ}$



### Data Detection

- Data detection uses the same front end as the channel estimation phase
- To detect the symbol we use the  $A_{DS}$  and  $H_{ch}$  matching filter that was found in channel estimation stage
- The maximum likelihood estimator under additive Gaussian noise is given by the frequency domain
- Hard decoding is applied on  $\hat{s}_{soft}$  by finding the nearest QPSK symbol

$$Y[k] = sH[k]A_{DS}[k] + Z[k], k \in \mathcal{L}$$

$$R[k] = s + \frac{A_{DS}^*[k]H^*[k]}{\|H[k]\|^2 \|A_{DS}[k]\|^2} Z[k], k \in \mathcal{L}$$

$$\hat{s}_{soft} = \frac{1}{M} \sum_{k \in \mathcal{L}} R[k]$$

### Simulation Results

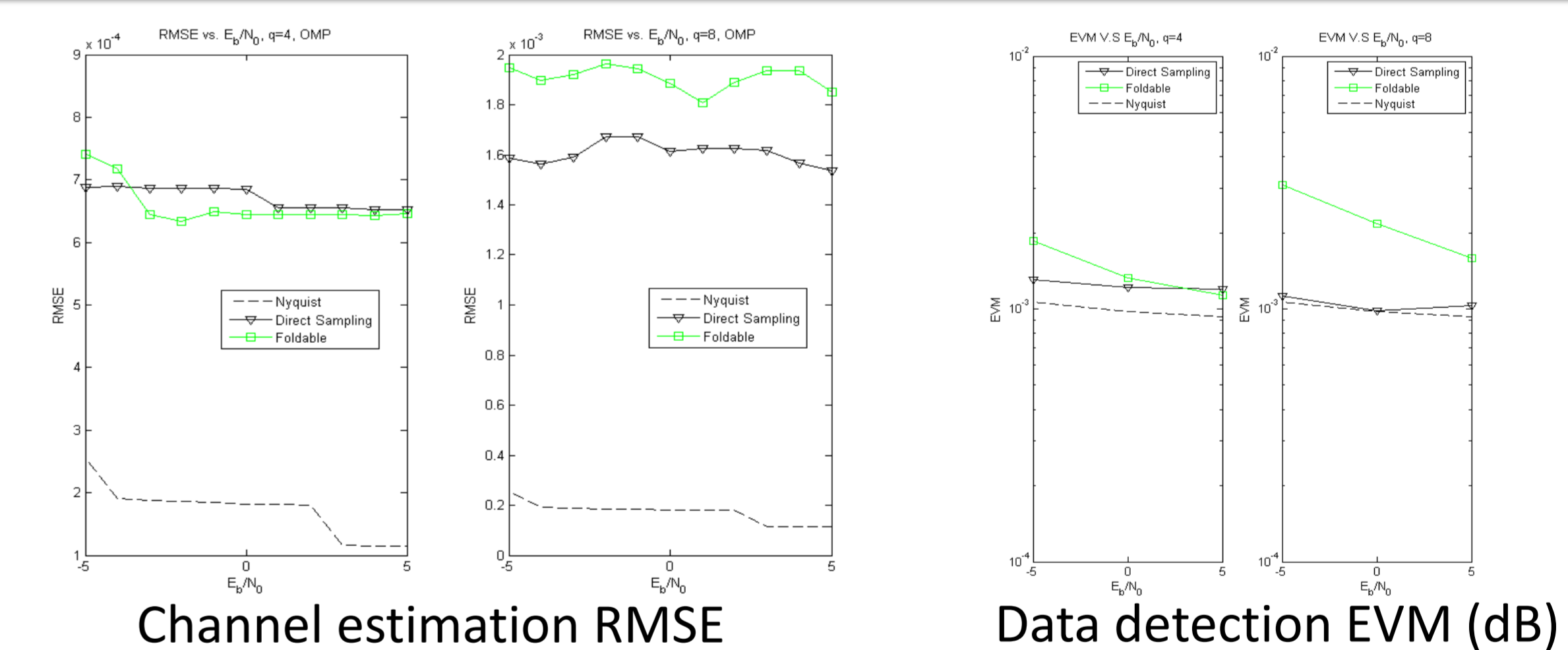
- Matlab simulation compare results for Nyquist, Foldable and \*Direct sample methods
- \*Direct FFT Sampling: Randomly select M coefficients to sample from full rate (not feasible)
- Measuring performance using energy capture and RMS error:
- Performance of data detection through Error Vector Magnitude (EVM):

$$RMSE(h, \hat{h}) = \sqrt{\frac{1}{N} \sum_{n=0}^{N-1} |h_{T,n} - \hat{h}_{T,n}|^2}$$

$$EVM(s, \hat{s}) = \frac{1}{J} \sqrt{\sum_{i=1}^J \|s_i - \hat{s}_i\|^2}$$

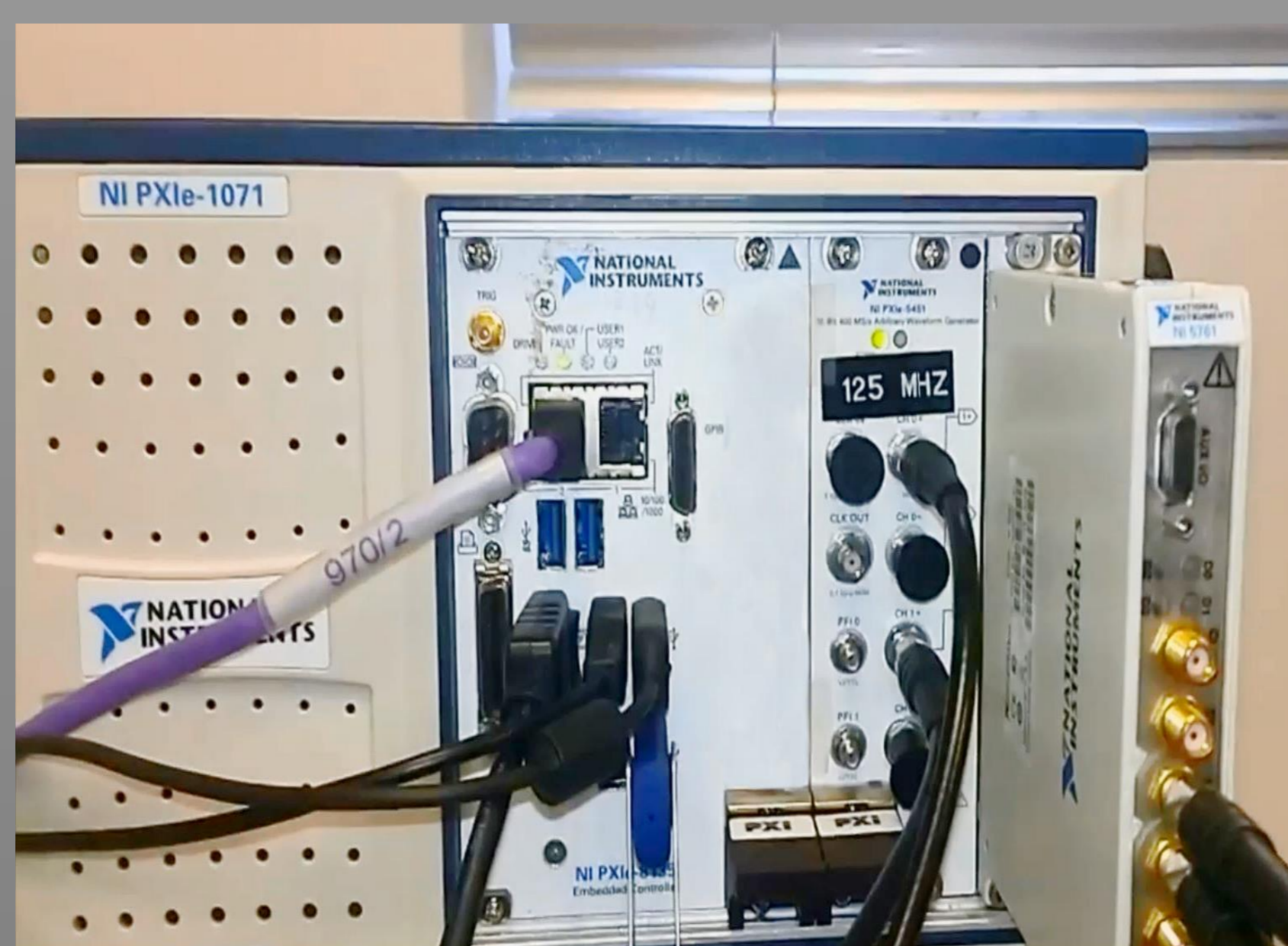
### Conclusions:

**Analog acquisition using a low rate ADC and standard front-end can be performed to detect data in multipath channels. For q=8, only 12% of the energy is dropped at estimation and EVM raised by factor 2 only at EbN0 of 0dB at data detection stage**



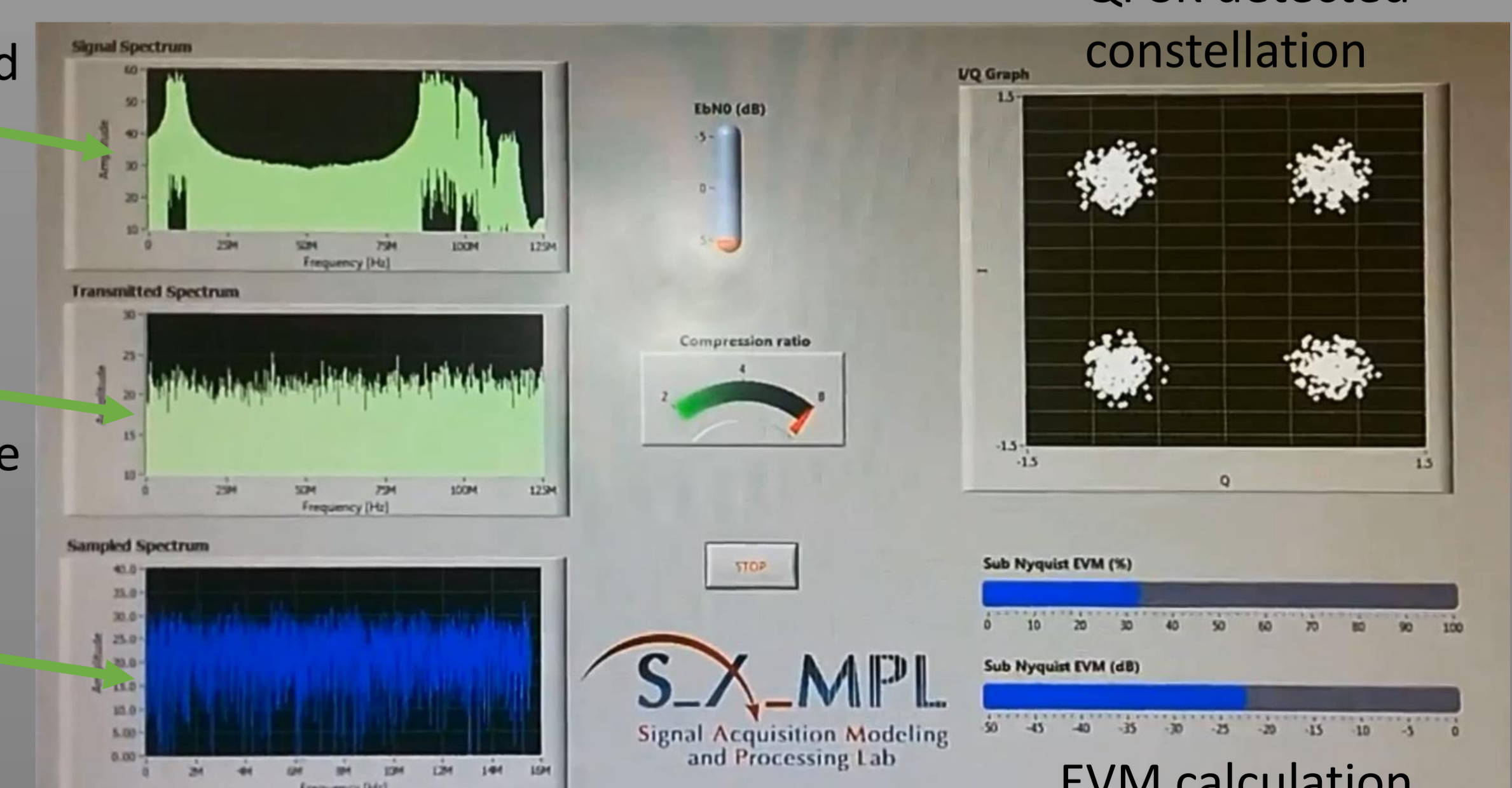
### System Implementation

- The demo system illustrates the application of sub-Nyquist sampling to QPSK UWB signals
- In the system  $\sim 250$ Kbps data rate is applied, which spreads to 125 MHz bandwidth
- 2 channels are active for I and Q in both AWG and sampler
- The channel response and noise are modeled before the packet transmitted through AWG
- The system implemented on NI PXIe chassis with signal generator – NI PXIe-5451 AWG and receiver – NI 5761 digitizer samples the signals directly at 125/64/32 MSps to achieve down to 1/8 of the signal's Nyquist rate



### Demo system

- Foldable generated signal
- Transmitted signal with channel response and noise
- Aliased signal as sampled by  $1/q$  Nyquist rate



### References

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